

Puzzles

RPN

1. Using all the numbers 0 1 2 3 4 5 6 7 8 9 10 and all the operators + + + + and - - - - - exactly once, write an RPN expression with maximal value. (Example: using 1 2 3 and + -, the largest expression value is $3\ 1\ -\ 2\ +\ =\ 4$)
2. Similar to problem #1, what is the *minimal* possible value?
3. Given a solution to #1, can you swap two numbers in your expression without changing the value? (e.g. $2\ 1\ -\ 3\ +\ =\ 4$)
4. Follow up to #3 – if the answer is “yes”, count how many different expressions have the same value, where the *order* of numbers and operators is the same, but the numbers’ values can be rearranged. (e.g. $1\ 2\ 3\ 4\ +\ +\ +$ and $4\ 2\ 3\ 1\ +\ +\ +$ are the same)

Binary Search

1. If you play the clock game (binary search) to guess an integer in the range $[1, 1023]$, what is the maximum number of guesses required? What are three numbers that require that many guesses?
2. Playing the clock game, over a min-max range of $[1, 1023]$, write a formula for $g(n)$ where $g(n)$ is the number of prices that require exactly n guesses. *Follow-up* does the range effect the definition of $g()$?
3. (Follow up to #2) – for the range $[1, 1023]$, what is the expected (average) number of guesses needed to win, assuming each price is equally likely?