

## Sorting Practice

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The following method is a correct implementation of the insertion sort algorithm. The method correctly sorts the elements of `numList` so that they appear in order from least to greatest.

```
public static void insertionSort(ArrayList<Integer> numList)
{
    for (int j = 1; j < numList.size(); j++)
    {
        int temp = numList.get(j);
        int k = j;
        while (k > 0 && temp < numList.get(k - 1))
        {
            numList.set(k, numList.get(k - 1));
            k--;
        }
        numList.set(k, temp);
        /* end of outer loop */
    }
}
```

Assume that `insertionSort` has been called with an `ArrayList` parameter that has been initialized with the following `Integer` objects.

[60, 30, 10, 20, 50, 40]

## Sorting Practice

1. What will the contents of `numList` be after three passes of the outer loop (i.e., when `j == 3` at the point indicated by `/* end of outer loop */`)?
- (A) [10, 20, 30, 50, 60, 40]
- (B) [10, 20, 30, 60, 50, 40]
- (C) [10, 30, 60, 20, 50, 40]
- (D) [20, 10, 30, 60, 50, 40]
- 

Consider the following method. This method correctly sorts the elements of array `data` into increasing order.

```
public static void sort(int[] data)
{
    for (int j = 0; j < data.length - 1; j++)
    {
        int m = j;
        for (int k = j + 1; k < data.length; k++)
        {
            if (data[k] < data[m]) /* Compare values */
            {
                m = k;
            }
        }
        int temp = data[m]; /* Assign to temp */
        data[m] = data[j];
        data[j] = temp;
        /* End of outer loop */
    }
}
```

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**Sorting Practice**

2. Assume that `sort` is called with the array `{6, 3, 2, 5, 4, 1}`. Which of the following represents the contents of `data` after three passes of the outer loop (i.e., when `j == 2` at the point indicated by `/* End of outer loop */`)?
- (A) `{1, 2, 3, 4, 5, 6}`
- (B) `{1, 2, 3, 5, 4, 6}`
- (C) `{1, 2, 3, 6, 5, 4}`
- (D) `{1, 3, 2, 5, 4, 6}`

**Sorting Practice**

3. Assume that `sort` is called with the array `{1, 2, 3, 4, 5, 6}`. How many times will the expression indicated by `/* Compare values */` and the statement indicated by `/* Assign to temp */` execute?

(A)

|                                   |                                   |
|-----------------------------------|-----------------------------------|
| <code>/* Compare values */</code> | <code>/* Assign to temp */</code> |
| 15 times                          | 5 times                           |

(B)

|                                   |                                   |
|-----------------------------------|-----------------------------------|
| <code>/* Compare values */</code> | <code>/* Assign to temp */</code> |
| 15 times                          | 6 times                           |

(C)

|                                   |                                   |
|-----------------------------------|-----------------------------------|
| <code>/* Compare values */</code> | <code>/* Assign to temp */</code> |
| 21 times                          | 5 times                           |

(D)

|                                   |                                   |
|-----------------------------------|-----------------------------------|
| <code>/* Compare values */</code> | <code>/* Assign to temp */</code> |
| 21 times                          | 6 times                           |

## Sorting Practice

The following method is a correct implementation of the selection sort algorithm. The method sorts the elements of `arr` so that they are in order from least to greatest.

```
public static void selectionSort(int[] arr)
{
    for (int j = 0; j < arr.length - 1; j++)
    {
        int minIndex = j;
        for (int k = j + 1; k < arr.length; k++)
        {
            if (arr[k] < arr[minIndex])
            {
                minIndex = k;
            }
        }

        int temp = arr[j];
        arr[j] = arr[minIndex];
        arr[minIndex] = temp;
        /* end of outer loop */
    }
}
```

Assume that `selectionSort` has been called with an `int[]` argument that has been initialized with the following contents.

```
{40, 30, 50, 60, 10, 20}
```

**Sorting Practice**

4. What will the contents of `arr` be after three iterations of the outer loop (i.e., when `j == 2` at the point indicated by `/* end of outer loop */`)?
- (A) {10, 20, 30, 40, 60, 50}
- (B) {10, 20, 30, 60, 40, 50}
- (C) {10, 20, 50, 60, 40, 30}
- (D) {10, 30, 50, 60, 40, 20}
-

## Sorting Practice

Consider the following correct implementation of the selection sort algorithm.

```
public static void selectionSort(int[] elements)
{
    for (int j = 0; j < elements.length - 1; j++)
    {
        int minIndex = j;
        for (int k = j + 1; k < elements.length; k++)
        {
            if (elements[k] < elements[minIndex])
            {
                minIndex = k;
            }
        }
        if (j != minIndex)
        {
            int temp = elements[j];
            elements[j] = elements[minIndex];
            elements[minIndex] = temp;    // Line 17
        }
    }
}
```

The following declaration and method call appear in a method in the same class as `selectionSort`.

```
int[] arr = {9, 8, 7, 6, 5};
selectionSort(arr);
```

5. How many times is the statement in line 17 of the method executed as a result of the call `selectionSort(arr)`?
- (A) 2
  - (B) 3
  - (C) 4
  - (D) 5
- 
-

## Sorting Practice

The following method is intended to sort an array of integers into ascending order.

```
public static void sort(int[] arr)
{
    for (int j = 0; j < arr.length - 1; j++)
    {
        int minIndex = j;
        for (int k = j + 1; k < arr.length - 1; k++)
        {
            if (arr[k] < arr[minIndex])
            {
                minIndex = k;
            }
        }
        int temp = arr[minIndex];
        arr[minIndex] = arr[j];
        arr[j] = temp;
    }
}
```

6. This method works as intended for some, but not all, `int` arrays. Which of the following arrays can be used to show that the method does not work as intended?
- (A) {1, 2, 3, 4, 5}
- (B) {1, 2, 3, 5, 4}
- (C) {1, 2, 4, 3, 5}
- (D) {1, 3, 2, 4, 5}
- 
-

## Sorting Practice

The following method is a correct implementation of the insertion sort algorithm. The method correctly sorts the elements of `arr` so that they appear in order from least to greatest.

```
public static void insertionSort(int[] arr)
{
    for (int j = 1; j < arr.length; j++)
    {
        int temp = arr[j];
        int possibleIndex = j;
        while (possibleIndex > 0 && temp < arr[possibleIndex - 1])
        {
            arr[possibleIndex] = arr[possibleIndex - 1];
            possibleIndex--;           // Line 10
        }
        arr[possibleIndex] = temp;
    }
}
```

The following code segment appears in a method in the same class as `insertionSort`.

```
int[] numbers = {4, 12, 4, 7, 19, 6};
insertionSort(numbers);
```

7. How many times is the statement in line 10 of the method executed as a result of the call to `insertionSort`?
- (A) 2
  - (B) 3
  - (C) 4
  - (D) 5
-

## Sorting Practice

The following method is a correct implementation of the selection sort algorithm. The method correctly sorts the elements of `data` so that they appear in order from least to greatest.

```
public static void selectionSort(int[] data)
{
    for (int j = 0; j < data.length - 1; j++)
    {
        int minIndex = j;

        for (int k = j + 1; k < data.length; k++)
        {
            if (data[k] < data[minIndex])
            {
                minIndex = k;    // Line 11
            }
        }

        if (j != minIndex)
        {
            int temp = data[j];
            data[j] = data[minIndex];
            data[minIndex] = temp;
        }
    }
}
```

The following code segment appears in a method in the same class as `selectionSort`.

```
int[] vals = {5, 10, 2, 1, 12};
selectionSort(vals);
```

8. How many times is the statement in line 11 of the method executed as a result of the call to `selectionSort`?
- (A) 1
  - (B) 2
  - (C) 3
  - (D) 4
- 
-

## Sorting Practice

The following method is a correct implementation of the selection sort algorithm. The method correctly sorts the elements of `arr` so that they appear in order from least to greatest.

```
public static void selectionSort(int[] arr)
{
    for (int j = 0; j < arr.length - 1; j++)
    {
        int minIndex = j;
        for (int k = j + 1; k < arr.length; k++)
        {
            if (arr[k] < arr[minIndex])
            {
                minIndex = k;
            }
        }
        int temp = arr[j];
        arr[j] = arr[minIndex];
        arr[minIndex] = temp;
        /* end of outer loop */
    }
}
```

9. Which of the following could be the contents of `arr` after two passes of the outer loop (i.e., when `j == 1` at the point indicated by `/* end of outer loop */`)?
- (A) {10, 20, 50, 40, 30}
- (B) {10, 30, 50, 40, 20}
- (C) {20, 10, 50, 40, 30}
- (D) {20, 30, 50, 40, 10}

## Sorting Practice

10. Consider the static method `selectSort` shown below. Method `selectSort` is intended to sort an array into increasing order; however, it does not always work as intended.

```
// precondition: numbers.length > 0

// postcondition: numbers is sorted in increasing order

public static void selectSort(int[] numbers)
{
    int temp;

Line 1:   for (int j = 0; j < numbers.length - 1; j++)
        {

Line 2:   int pos = 0;

Line 3:   for (int k = j + 1; k < numbers.length; k++)
            {

Line 4:   if (numbers[k] < numbers[pos])
                {

Line 5:   pos = k;
                }
            }

        temp = numbers[j];
        numbers[j] = numbers[pos];
        numbers[pos] = temp;
    }
}
```

Which of the following changes should be made so that `selectSort` will work as intended?

**Sorting Practice**

- (A) Line 1 should be changed to  
for (int j = 0; j < numbers.length - 2; j++)
- (B) Line 2 should be changed to  
int pos = j;
- (C) Line 3 should be changed to  
for (int k = 0; k < numbers.length; k++)
- (D) Line 4 should be changed to  
if (numbers[k] > numbers[pos])

**Sorting Practice**

11. The following incomplete method is intended to sort its array parameter `arr` in increasing order.

```
// postcondition: arr is sorted in increasing order

public static void sortArray(int[] arr)
{
    int j, k;

    for (j = arr.length - 1; j > 0; j--)
    {
        int pos = j;

        for ( /* missing code */ )
        {
            if (arr[k] > arr[pos])
            {
                pos = k;
            }
        }

        swap(arr, j, pos);
    }
}
```

Assume that `swap(arr, j, pos)` exchanges the values of `arr[j]` and `arr[pos]`. Which of the following could be used to replace `/* missing code */` so that executing the code segment sorts the values in array `arr`?

**Sorting Practice**

- (A) `k = j - 1; k > 0; k--`
  - (B) `k = j - 1; k >= 0; k--`
  - (C) `k = 1; k < arr.length; k++`
  - (D) `k = 0; k <= arr.length; k++`
- 

Consider the following correct implementation of the selection sort algorithm.

```
public static void selectionSort(int[] elements)
{
    for (int j = 0; j < elements.length - 1; j++)
    {
        int minIndex = j;
        for (int k = j + 1; k < elements.length; k++)
        {
            if (elements[k] < elements[minIndex])
            {
                minIndex = k;
            }
        }
        if (j != minIndex)
        {
            int temp = elements[j];
            elements[j] = elements[minIndex];
            elements[minIndex] = temp; // line 17
        }
    }
}
```

The following declaration and method call appear in a method in the same class as `selectionSort`.

```
int[] arr = {30, 40, 10, 50, 20};
selectionSort(arr);
```

12. How many times is the statement `elements[minIndex] = temp;` in line 17 of the method executed as a result of the call to `selectionSort`?
- (A) 2
  - (B) 3
  - (C) 4
  - (D) 5
-

## Sorting Practice

13. Consider the following `mergeSortHelper` method, which is part of an algorithm to recursively sort an array of integers.

```
/** Precondition: (arr.length == 0 or 0 <= from <= to <= arr.length)
 * arr.length == temp.length
 */
public static void mergeSortHelper(int[] arr,
    int from, int to, int[] temp)
{
    if (from < to)
    {
        int middle = (from + to) / 2;
        mergeSortHelper(arr, from, middle, temp);
        mergeSortHelper(arr, middle + 1, to, temp);
        merge(arr, from, middle, to, temp);
    }
}
```

The `merge` method is used to merge two halves of an array (`arr[from]` through `arr[middle]`, inclusive, and `arr[middle + 1]` through `arr[to]`, inclusive) when each half has already been sorted into ascending order. For example, consider the array `arr1`, which contains the values `{1, 3, 5, 7, 2, 4, 6, 8}`. The lower half of `arr1` is sorted in ascending order (elements `arr1[0]` through `arr1[3]`, or `{1, 3, 5, 7}`), as is the upper half of `arr1` (elements `arr1[4]` through `arr1[7]`, or `{2, 4, 6, 8}`). The array will contain the values `{1, 2, 3, 4, 5, 6, 7, 8}` after the method call `merge(arr1, 0, 3, 7, temp)`. The array `temp` is a temporary array declared in the calling program.

Consider the following code segment, which appears in a method in the same class as `mergeSortHelper` and `merge`.

```
int[] vals = {80, 50, 30, 20, 60, 70};
int[] temp = new int[vals.length];
mergeSortHelper(vals, 0, vals.length - 1, temp);
```

Which of the following represents the arrays merged the last time the `merge` method is executed as a result of the code segment above?

- (A) `{20, 30, 50}` and `{60, 70, 80}` are merged to form `{20, 30, 50, 60, 70, 80}`.
- (B) `{20, 50, 70}` and `{30, 60, 80}` are merged to form `{20, 30, 50, 60, 70, 80}`.
- (C) `{20, 50, 70}` and `{30, 60, 80}` are merged to form `{20, 50, 70, 30, 60, 80}`.
- (D) `{30, 50, 80}` and `{20, 60, 70}` are merged to form `{20, 30, 50, 60, 70, 80}`.

## Sorting Practice

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Consider the following `mergeSortHelper` method, which is part of a correctly implemented algorithm to recursively sort an array of integers.

```
/** Preconditions: (arr.length == 0 or
 *      0 <= from <= to <= arr.length)
 *      arr.length == temp.length
 */
public static void mergeSortHelper(int[] arr, int from,
                                   int to, int[] temp)
{
    if (from < to)
    {
        int middle = (from + to) / 2;
        mergeSortHelper(arr, from, middle, temp);
        mergeSortHelper(arr, middle + 1, to, temp);
        merge(arr, from, middle, to, temp);
    }
}
```

The `merge` method (not shown) is used to merge two halves of an array (`arr[from]` through `arr[middle]`, inclusive, and `arr[middle + 1]` through `arr[to]`, inclusive) when each half has already been sorted into ascending order. For example, if `arr1` contains `{1, 3, 5, 7, 2, 4, 6, 8}`, then `arr1` will contain `{1, 2, 3, 4, 5, 6, 7, 8}` after the method call `merge(arr1, 0, 3, 7, temp)`.

Consider the following code segment, which appears in a method in the same class as `mergeSortHelper` and `merge`.

```
int[] numbers = {40, 10, 20, 30};
int[] temp = new int[numbers.length];
mergeSortHelper(numbers, 0, numbers.length - 1, temp);
```

14. How many times will the `merge` method be called as a result of running the code segment?
- (A) 1
  - (B) 2
  - (C) 3
  - (D) 4
-